

Planetary and Lunar Ephemerides : from tests of SEP and graviton to ITLN

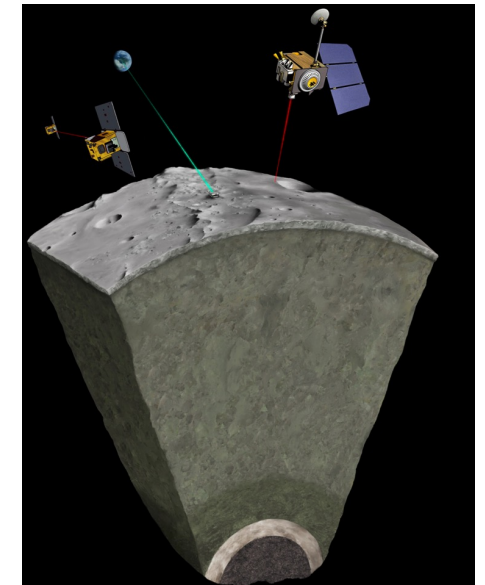
Agnès Fienga^(1,2)

Olivier Minazzoli^(3,4), V. Mariani⁽¹⁾, A. Hees⁽⁵⁾, L. Bernus⁽²⁾, L.
Bigot⁽⁶⁾, A. Di Ruscio^(1,7), D. Durante⁽⁷⁾, M. Gastineau⁽²⁾, J. Laskar⁽²⁾

L. Iess⁽⁷⁾

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⁽⁶⁾ OCA, Lagrange, UCA ⁽⁷⁾ CRAS, Sapienza, Rome

-
- 1) INPOP update in 2023
 - 2) New results for graviton and SEP
 - 3) ITLN



Journées des systèmes de référence spatio-temporels 2023
"Time and General Relativity"
11-13 September 2023, Nice (France)



1) INPOP update in 2023

2) New results for graviton and SEP

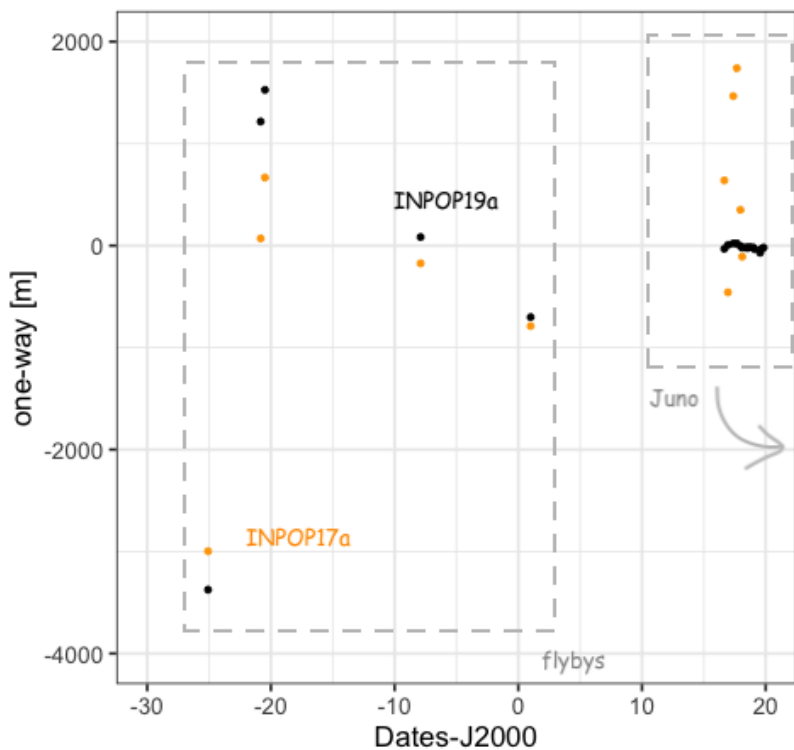
3) ITLN

INPOP update in 2023

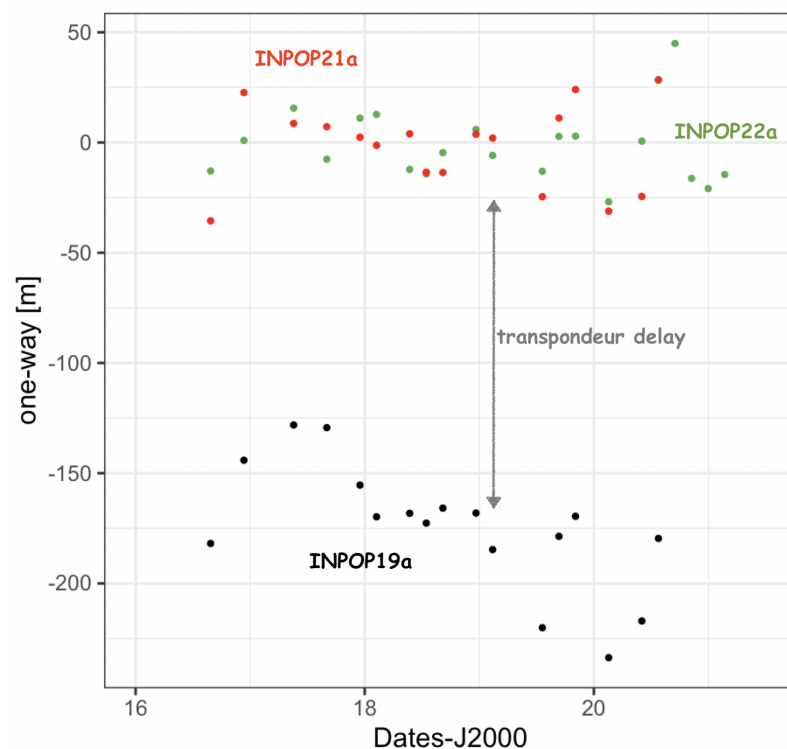
- **Juno CRAS range analysis from 2016 to 2021.5**
- **INPOP23a : Juno VLBA**
- Gain on Jupiter orbit accuracy : from 2 km (17a) to 20 m.
- MEX additional set

	INPOP17a 2018	INPOP19a 2019	INPOP20a/21a/22a 2020/2021
Dynamics			
MBA	343 + 1 ring	343	343
TNO	none	3 rings + 9 ind	509 ind
Lense-Thirring	N	N	Y
Fit			
Parameters	210	402	402
GM _A	152	343	343
Method	BVLS	BVLS + MC	BVLS + MC
Dataset	1913:2014	1924:2019.5	1924:2020.5/2021.5
Jupiter	2 km	20 m	20 m
Saturn	2004-2014	2004-2017	2004-2017
SSB shift / INPOP10e	0	94 km	94 km

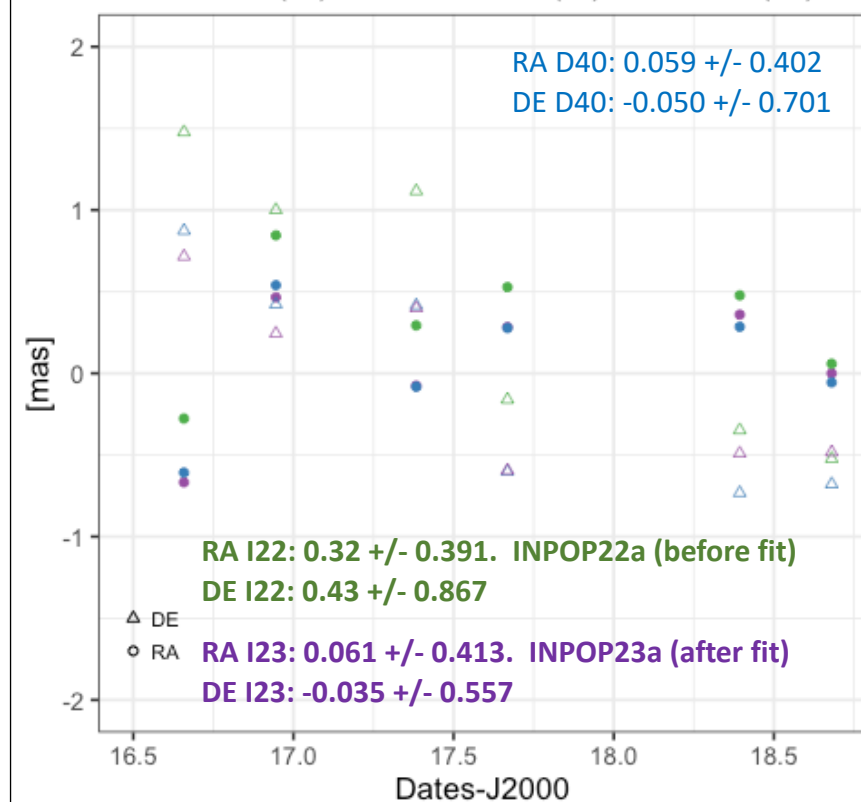
INPOP17a(O)+INPOP19a(B)



INPOP19a(B) + INPOP21a(R) + INPOP22a(G)



INPOP23a(M) + INPOP22a(G) + DE440(BI)



Comparisons with DE

Convergency of the models

$$\mathbf{I22a-D440} < \mathbf{I19a-D440} < \mathbf{I19a-D438}$$

	INPOP17a 2018	INPOP19a 2020	DE438 2018	DE440 2021
Dynamics				
MBA	343 i.m. + 1 ring	343 i.m.	343 i.m.	343 i.m.
TNO	none	3 rings + 9 ind I21a: 509 ind	none	1 ring + 36 ind
General Relativity	EIH	EIH + LT	EIH	EIH + LT
Fit				
GM _A	153 BVLS + 1 ring	343 MC	343 LS	343 LS
TNO	none	1 ring mass I21a: 1 mass @ 509 ind.	none	1 ring mass
Dataset	1913:2014	1924:2019.5 I21a: 1924:2020.5 I22a: 1924:2021.5	1924:2013+	1924:2020
SSB shift	0	94 km	0	≈ 100 km

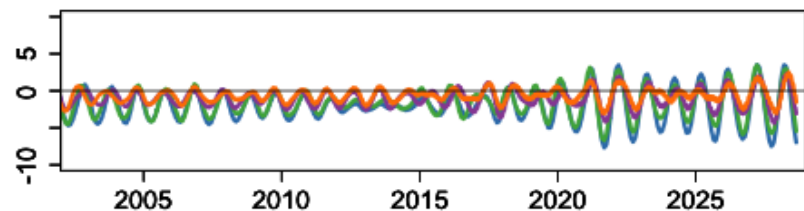
Comparisons with DE

Convergency of the models

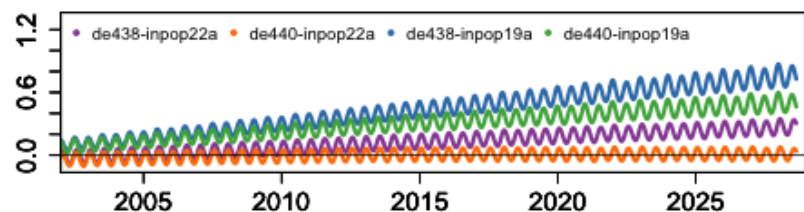
$$I22a-D440 < I19a-D440 < I19a-D438$$

Earth

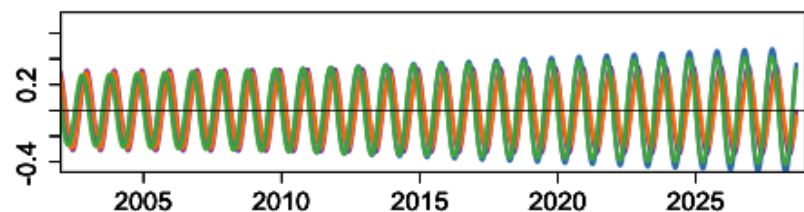
Diff HELIO DIST [m]



Diff HELIO LAT [mas]

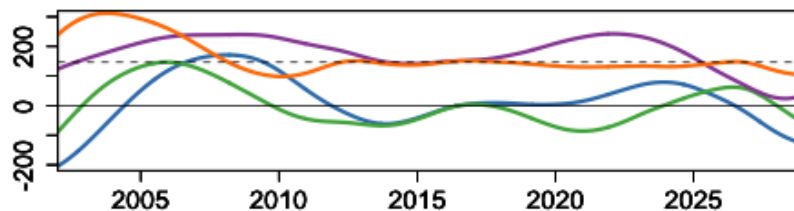


Diff HELIO LONG [mas]

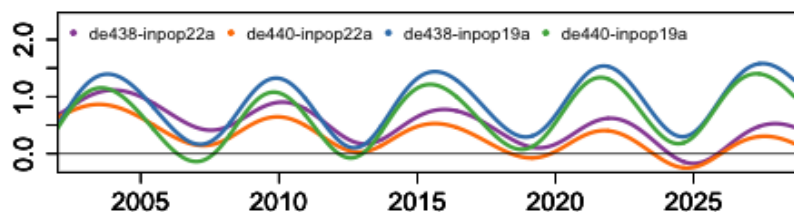


Jupiter B.

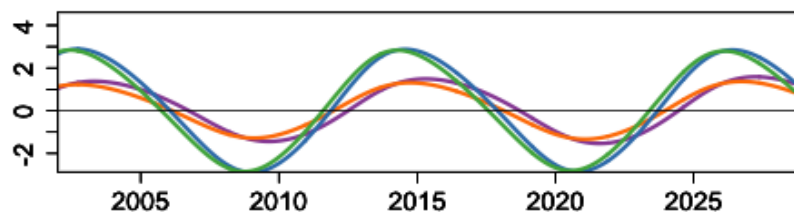
Diff HELIO DIST [m]



Diff HELIO LAT [mas]

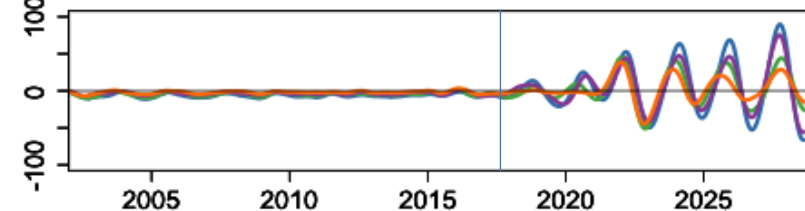


Diff HELIO LONG [mas]

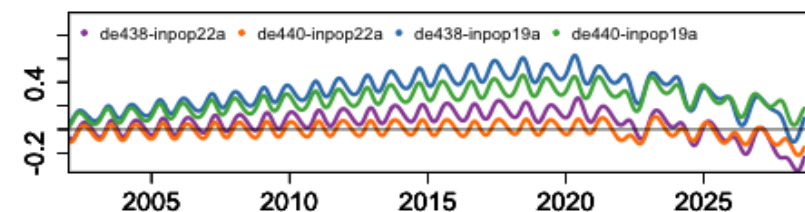


Mars

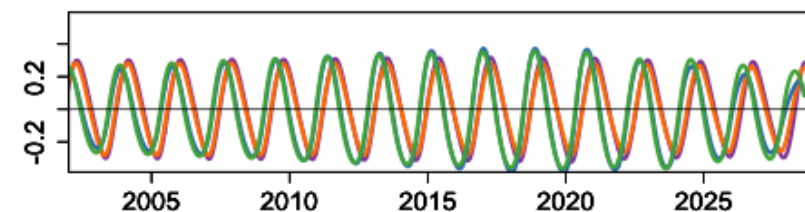
Diff HELIO DIST [m]



Diff HELIO LAT [mas]



Diff HELIO LONG [mas]



● INPOP22a-DE440 ● INPOP22a-DE438 ● INPOP19a-DE438 ● INPOP19a-DE440

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- 1) INPOP update in 2023
 - 2) **New results for graviton and SEP**
 - 3) ITLN

New results for graviton (Will 2018, Bernus et al. 2019, 2020)

- What about if metric field has a mass, m_g ? or Yukawa suppression of massive interactions at the Compton length, λ_g such as:

$$\lambda_g = \frac{\hbar}{cm_g}$$

(Will, 2018) :

$$w = w_{\text{Newton}} \exp(-r/\lambda_g)$$

→

$$w = w_{\text{Newton}} \left(1 + \frac{1}{2} \frac{r^2}{\lambda_g^2} \right) + \mathcal{O}(\lambda_g^{-3}),$$

(Bernus et al. 2019)

- What about if the metric doesn't have a mass but an additional gravitational field does ? (Fifth force)

$$w = w_{\text{Newton}} (1 + \alpha \exp(-r/\lambda))$$

with

- α , the strenght of the force relative to gravity
- λ , the range of the force

B19 + 5thF :

$$\text{If } \alpha < 1 \text{ and } \lambda_g \gg r, \text{ then } \lambda_g \approx \frac{\lambda}{\sqrt{|\alpha|}}$$

Massive graviton / Yukawa suppression

(Mariani et al., Phys.Rev. D, 108:024047, Jul 2023)

$$w = w_{\text{Newton}} \left(1 + \frac{1}{2} \frac{r^2}{\lambda_g^2} \right) + \mathcal{O}(\lambda_g^{-3}),$$

(Bernus et al., 2019, 2021) (Mariani et al., 2023)

CL	GWTC-1		GWTC-3		INPOP17a		INPOP19a		INPOP21a	
	0.90	0.90	0.90	0.90	0.90	0.90	0.90	0.90	0.90	0.90
Graviton mass										
$\lambda_g \times 10^{-13}$ [km]	2.6	9.77	1.83	3.93	12.01	209.67				
$m_g \times 10^{23}$ [eV/c ²]	4.7	1.27	6.76	3.16	1.03	0.059				
Fifth Force										
$\frac{\lambda}{\sqrt{ \alpha }} \times 10^{-13}$ [km], $\alpha > 0$			1.83	3.93						
$\frac{\lambda}{\sqrt{ \alpha }} \times 10^{-13}$ [km], $\alpha < 0$				3.77						

(Mariani et al., 2023)

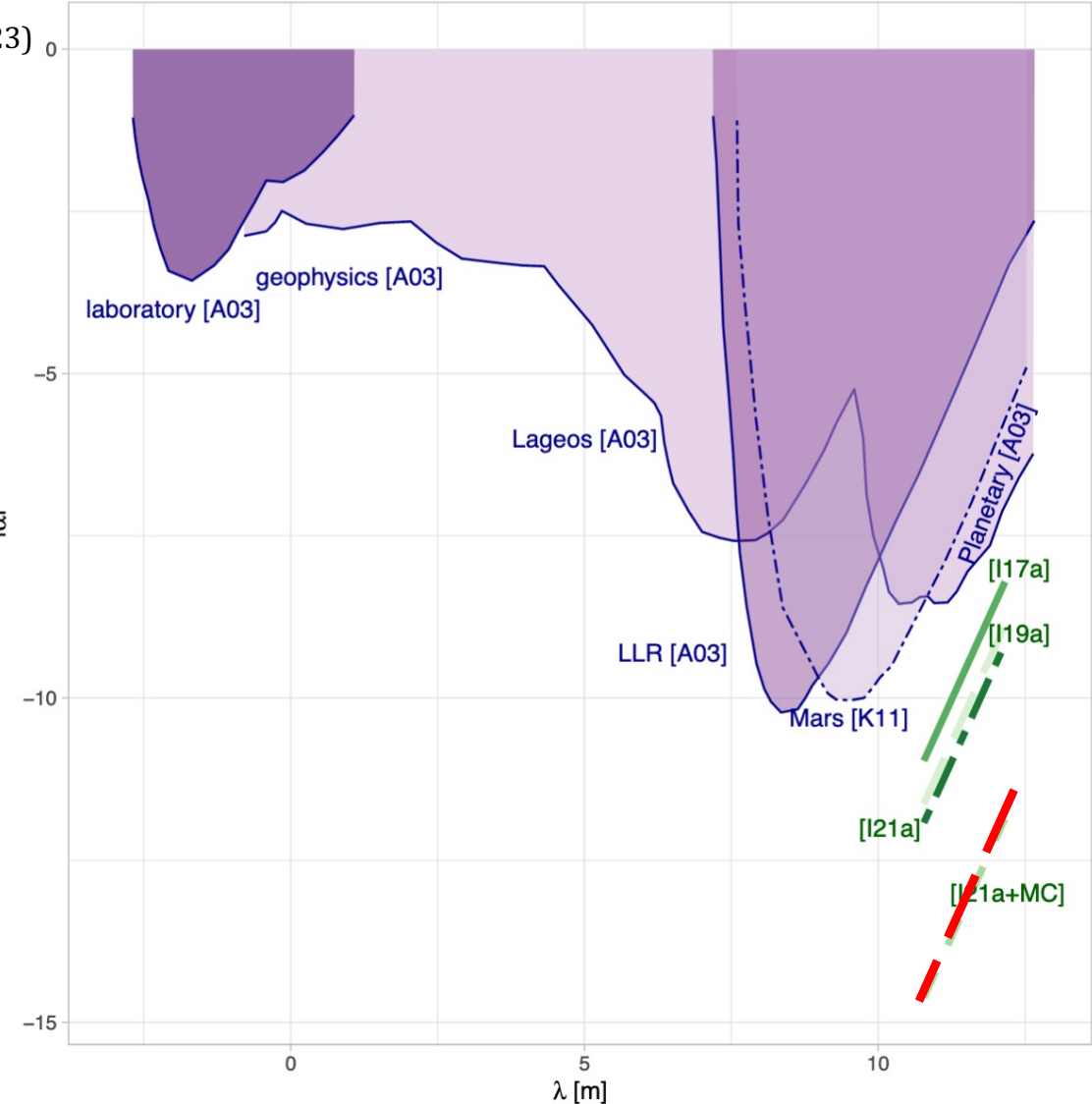
$$m_g < 0.10 \times 10^{-23} \text{ eV/c}^2 \text{ C.L. 99.7 \%}$$

$$\lambda_g > 122.48 \times 10^{13} \text{ km C.L. 99.7 \%}$$

(Will 2018):
postfit analysis

$$m_g < 0.40 - 0.8 \times 10^{23} \text{ eV/c}^2$$

$$\lambda_g > 14 - 27 \times 10^{13} \text{ km}$$



Einstein massless dilaton : INPOP test (Bernus et al. 2022)

(Minazzoli and Hees, 2016)

- Generic formalism allowing both WEP, GWEP and SEP violation
- Non-universal coupling between scalar field and matter (linear or non-linear)
- Parameters of the metric $(\tilde{\alpha}, \beta_0)$ depend on dilatonic charges (proton, nucleon)

(Bernus et al. 2022)

- Introduction in INPOP of previous EIHDL and Shapiro modified equations
- Linear coupling ($d\beta_X = 0, \beta = 1$)
- Random exploration for α_G, α_T and α_0 starting with flat large priors
- Cost functions

	INPOP19a (Bernus et al. 22)	
Confidence:	90%	99.5%
$\alpha_0 (\times 10^5)$	-0.94 ± 5.35	1.01 ± 23.7
$\alpha_T (\times 10^6)$	0.24 ± 1.62	0.00 ± 24.5
$\alpha_G (\times 10^5)$	0.01 ± 4.38	-1.46 ± 12.0
$(\gamma - 1) \times 10^8$	0.2 ± 6	0.2 ± 11.2

$$g_{\mu\nu} = \frac{f_0}{f(\varphi)} g_{\mu\nu}^* \quad m_A^*(\phi) = \sqrt{\frac{f_0}{f(\varphi)}} m_A(\varphi).$$

$$\delta_A = \frac{\alpha_0 \tilde{\alpha}_A}{1 + \alpha_0^2}, \quad \delta_{AB} = \frac{\tilde{\alpha}_A \tilde{\alpha}_B}{1 + \alpha_0^2};$$

$$\mu_A = \frac{G}{f_0} (1 + \alpha_0^2) (1 + \delta_A) m_A(\varphi_0);$$

(Z)

$$\gamma = \frac{1 - \alpha_0^2}{1 + \alpha_0^2}, \quad \beta = 1 + \frac{\beta_0}{2} \frac{\alpha_0^2}{(1 + \alpha_0^2)^2};$$

(Bernus et al. 2022)

$$\begin{aligned} \mathbf{a}_T = & - \sum_{A \neq T} \frac{\mu_A}{r_{AT}^3} \mathbf{r}_{AT} (1 + \delta_T + \delta_{AT}) \\ & - \sum_{A \neq T} \frac{\mu_A}{r_{AT}^3 c^2} \mathbf{r}_{AT} \left\{ \gamma v_T^2 + (\gamma + 1) v_A^2 - 2(1 + \gamma) \mathbf{v}_A \cdot \mathbf{v}_T - \frac{3}{2} \left(\frac{\mathbf{r}_{AT} \cdot \mathbf{v}_A}{r_{AT}} \right)^2 - \frac{1}{2} \mathbf{r}_{AT} \cdot \mathbf{a}_A \right. \\ & \left. - 2(\gamma + \beta + d\beta_T) \sum_{B \neq T} \frac{\mu_B}{r_{TB}} - (2\beta + 2d\beta_A - 1) \sum_{B \neq A} \frac{\mu_B}{r_{AB}} \right\} \\ & + \sum_{A \neq T} \frac{\mu_A}{c^2 r_{AT}^3} [2(1 + \gamma) \mathbf{r}_{AT} \cdot \mathbf{v}_T - (1 + 2\gamma) \mathbf{r}_{AT} \cdot \mathbf{v}_A] (\mathbf{v}_T - \mathbf{v}_A) + \frac{3 + 4\gamma}{2} \sum_{A \neq T} \frac{\mu_A}{c^2 r_{AT}} \mathbf{a}_A \end{aligned}$$

$$c(t_r - t_e) = \frac{R}{c} + \sum_A (\gamma + 1 - \delta_A) \frac{\mu_A}{c^2} \ln \frac{\mathbf{n} \cdot \mathbf{r}_{rA} + r_{rA}}{\mathbf{n} \cdot \mathbf{r}_{eA} + r_{eA}}$$

Revised test with (Mariani et al, 2023b, arXiv:2310.00719)

(Minazzoli and Hees, 2016)

- Generic formalism allowing both WEP, GWEP and SEP violation
- Non-universal coupling between scalar field and matter (linear or non-linear)
- Parameters of the metric $(\tilde{\alpha}, \beta_0)$ depend on dilatonic charges (proton, nucleon)

$$(1 + \gamma - \delta_A)\mu_A = (1 + \gamma)\mu_A^I$$

$$\gamma = \frac{1 - \alpha_0^2}{1 + \alpha_0^2}, \quad \beta = 1 + \frac{\beta_0}{2} \frac{\alpha_0^2}{(1 + \alpha_0^2)^2}$$

From these equations, the Nordtvedt parameter η is now function of α_0

$$c(t_r - t_e) = \frac{R}{c} + \sum_A (\gamma + 1 - \delta_A) \frac{\mu_A}{c^2} \ln \frac{\mathbf{n} \cdot \mathbf{r}_{rA} + r_{rA}}{\mathbf{n} \cdot \mathbf{r}_{eA} + r_{eA}}$$

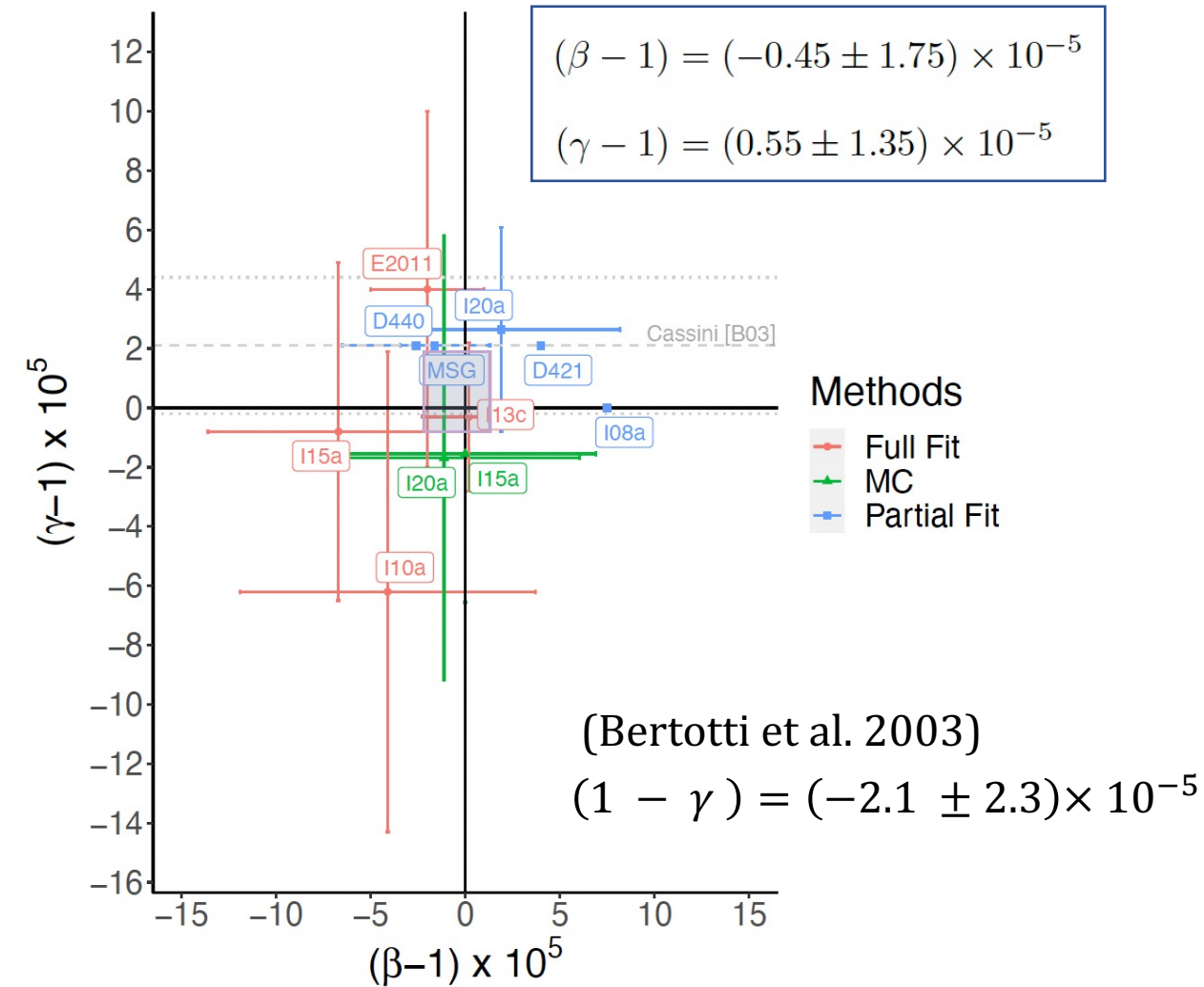
(Marini et al, 2023b, arXiv:2310.00719)

- INPOP21a
- MCMC on γ (Test A) : $\delta_A = 0$
- MCMC on γ with only the universal coupling of dilaton \rightarrow Brans-Dicke theory-like framework (Test B) $\rightarrow \eta$
- New SEP limit
- Limitation : $(1 - \gamma) > 0 ; \eta < 0$

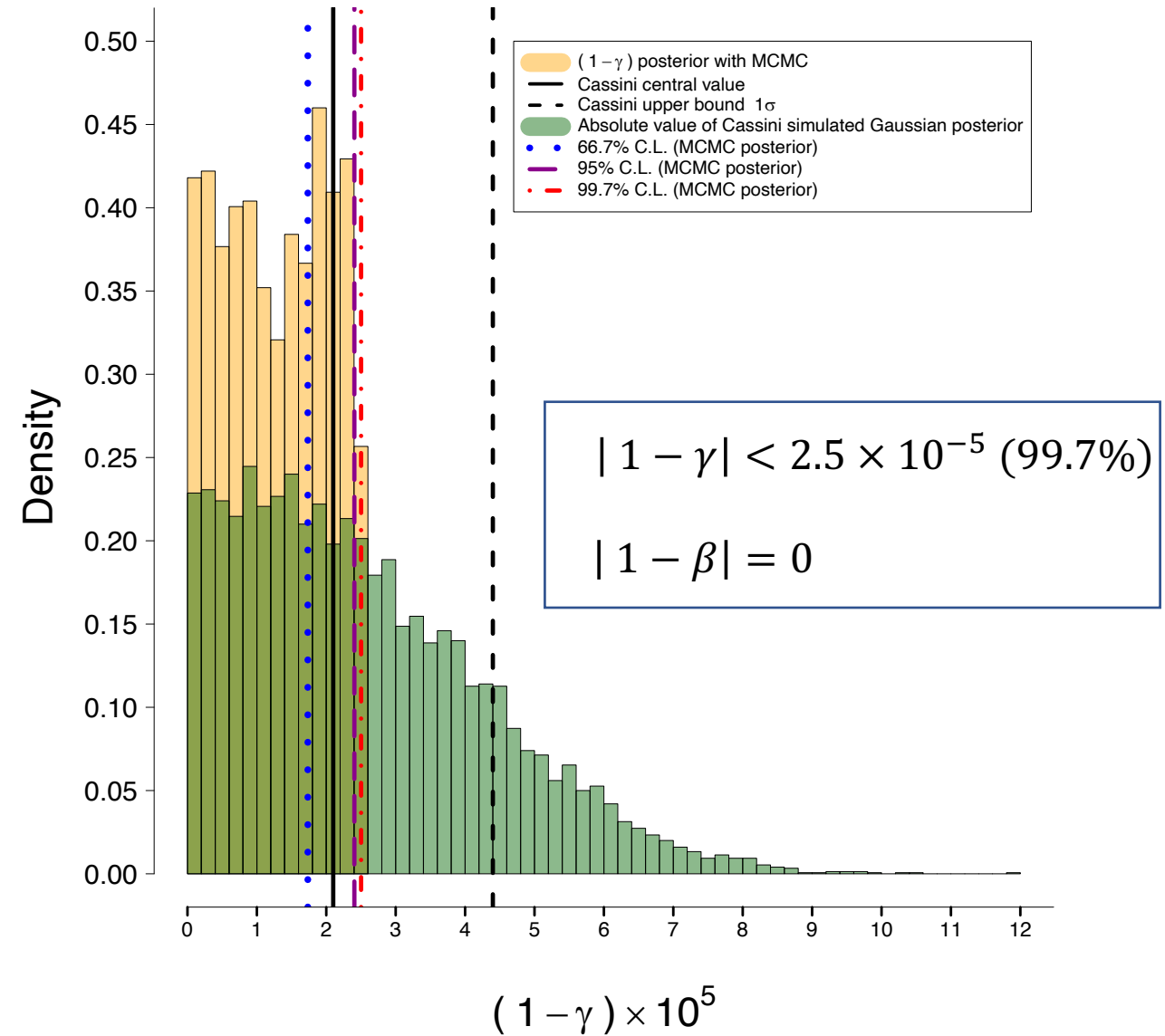
$$\eta = -(1 - \gamma) = -2 \frac{\alpha_0^2}{1 + \alpha_0^2}$$

Revised test with (Mariani et al, 2023b, arXiv:2310.00719)

(Fienga and Minazzoli, 2023)



Test A: MCMC on γ in PPN (without SEP, $\delta_A = 0$)



Revised test with (Mariani et al, 2023b, arXiv:2310.00719)

Test B : MCMC on γ with only the universal coupling of dilaton

- Brans-Dicke theory-like framework
- SEP

without SEP

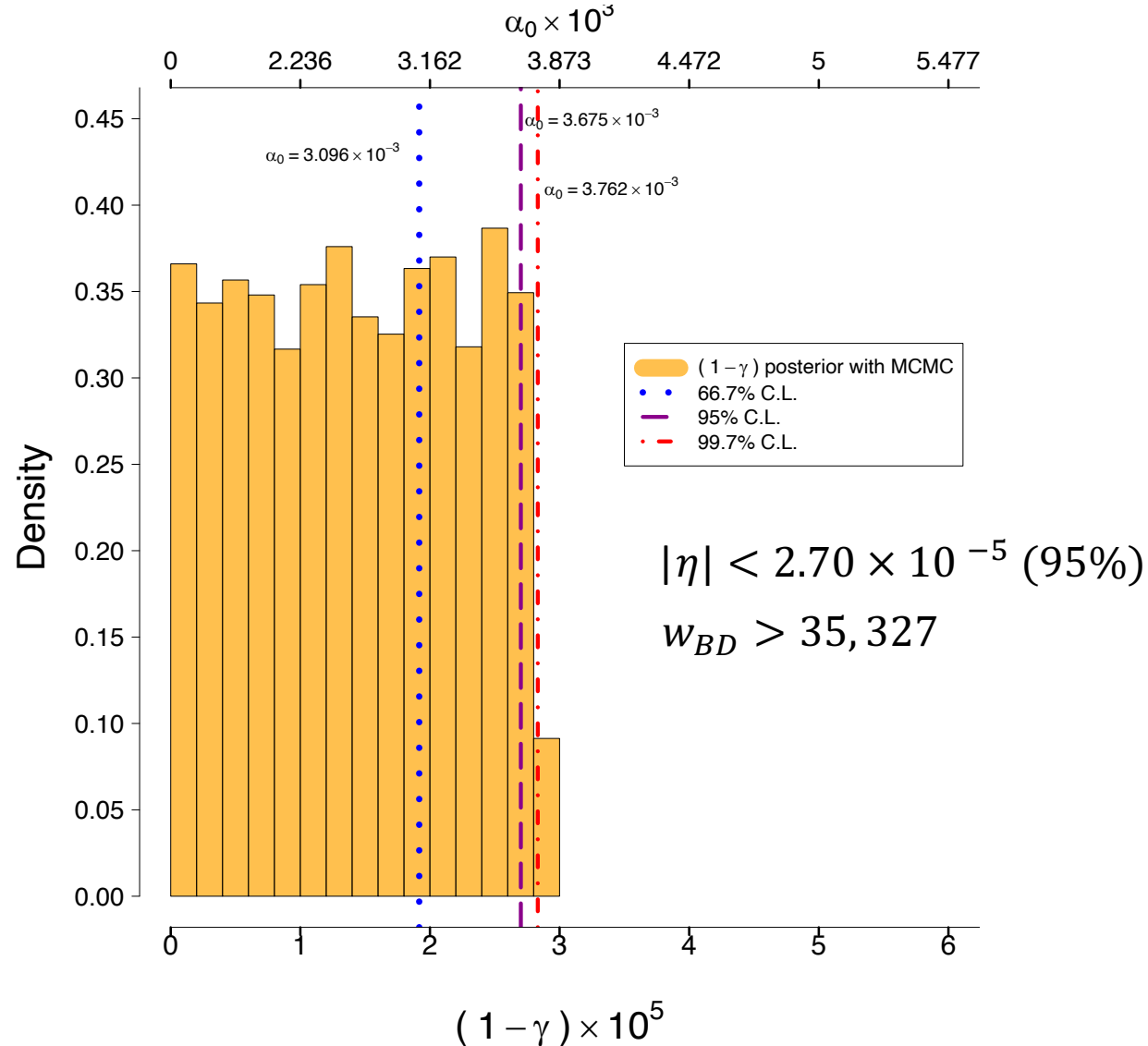
$$|\eta| < 2.5 \times 10^{-5} \text{ (99.7\%)}$$

with SEP

$$|\eta| < 2.8 \times 10^{-5} \text{ (99.7\%)}$$



Detectability of SEP
with planetary orbits



Messenger

(Genova et al. 2018)

$$\eta = (-5.48 \pm 7.3) \times 10^{-5}$$

LLR

(Viswanathan et al. 2018)

$$|\eta| < 30 \times 10^{-5}$$

Binary pulsar

(Voisin et al. 2020)

$$|\eta| < 0.76 \times 10^{-5} \text{ (95\%)}$$

$$w_{BD} > 140,000$$

-
- 1) INPOP update in 2023
 - 2) New results for graviton and SEP
 - 3) **ITLN: Interplanetary Laser Tri-lateration Network**

**Interplanetary Trilateration Workshop
Martin Johnson House
Scripps Institute of Oceanography, University of San Diego, CA
Feb 28 - Mar 1, 2023**

Interplanetary Laser Tri-lateration Network



PERGAMON

Journal of Geodynamics 34 (2002) 551–594

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Planetary and Space Science

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Asynchronous laser transponders for precise interplanetary ranging and time transfer

John J. Degnan

Geoscience Technology Office, Code 920.3, Laboratory for Terrestrial Physics,
NASA Goddard Space Flight Center, Greenbelt, MD 20771, USA

Sensitivity and antenna pattern for an interplanetary laser trilateration network

Bruce G. Bills  , Krzysztof M. Gorski

- Centimetric measurements of interplanetary distances
- (First) concept : Smith et al. 2018
- Recent sensitivity and feasibility studies: (Bills et al. 2022)
- Earth, Venus, Mars



journal homepage: www.elsevier.com/locate/pss



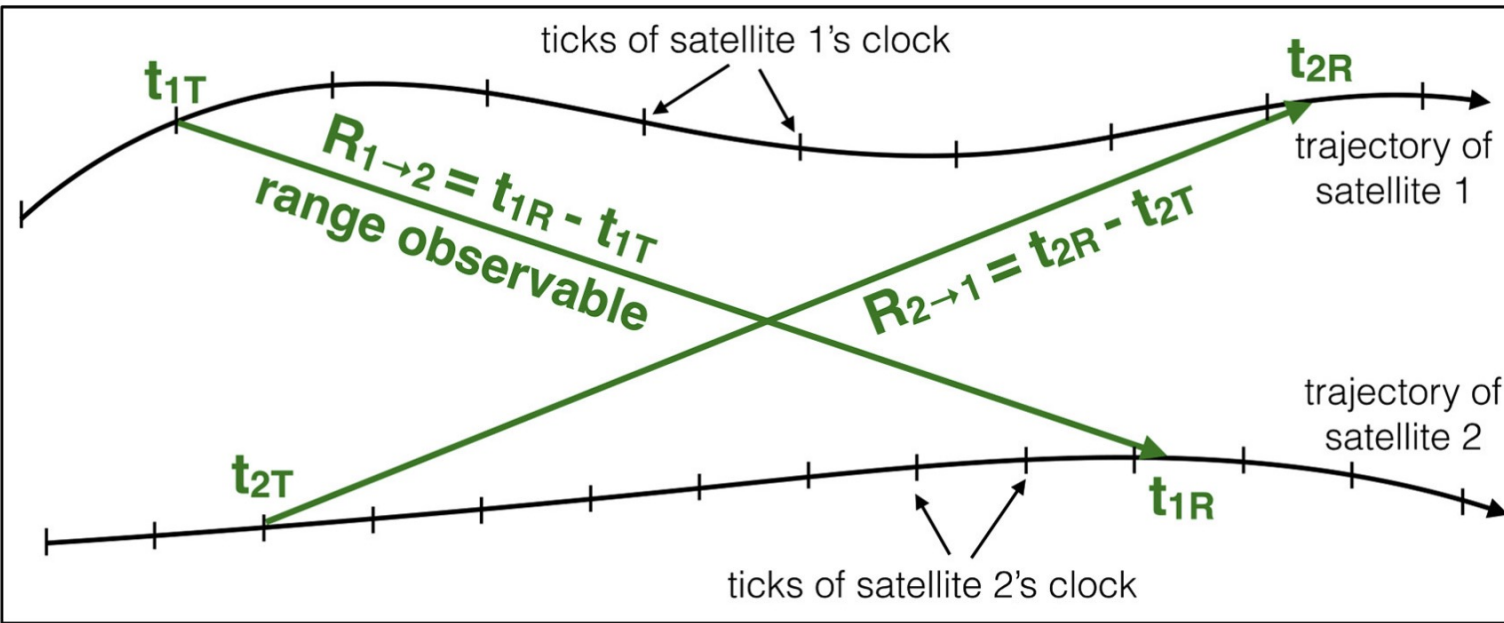
Trilogy, a planetary geodesy mission concept for measuring the expansion of the solar system



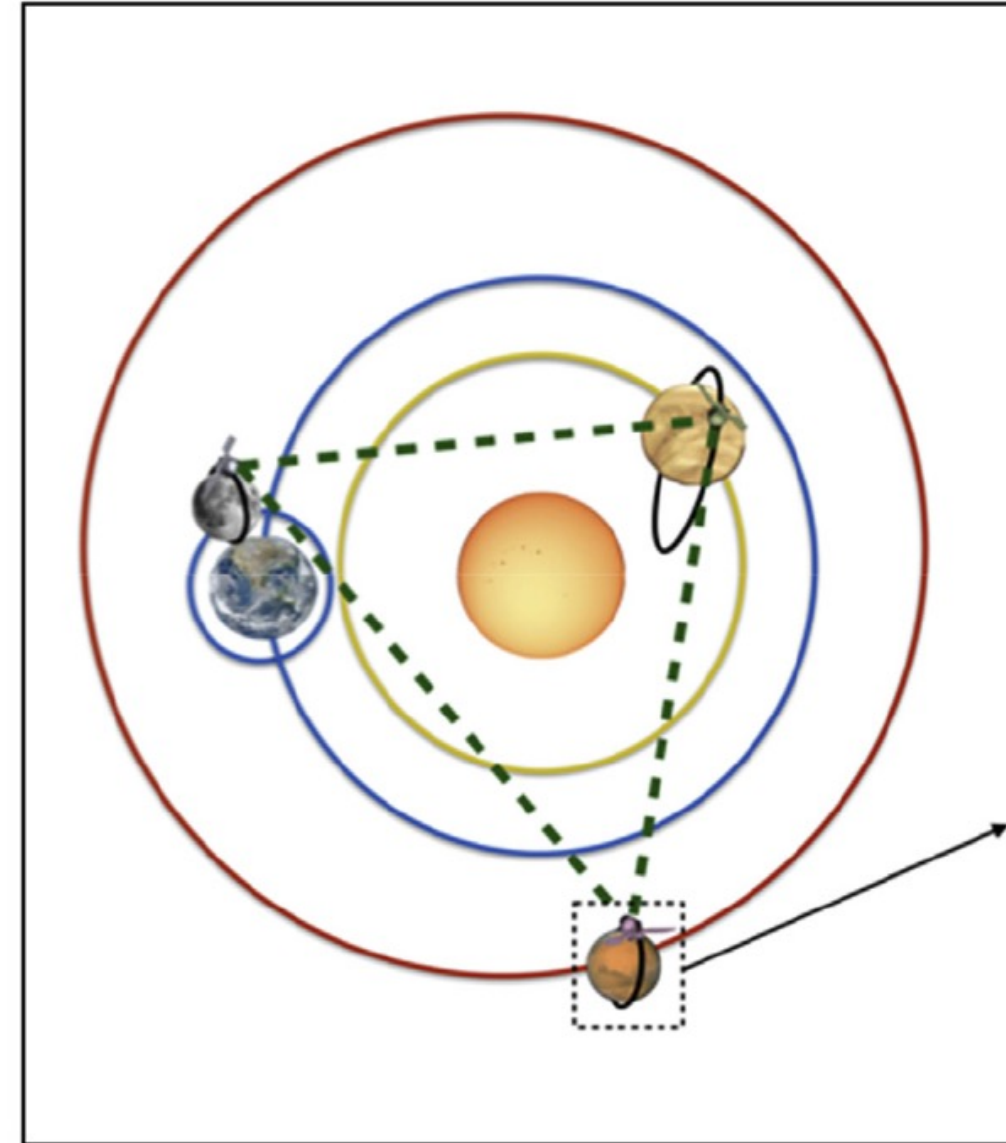
David E. Smith ^{a,*}, Maria T. Zuber ^a, Erwan Mazarico ^b, Antonio Genova ^a, Gregory A. Neumann ^b, Xiaoli Sun ^b, Mark H. Torrence ^c, Dan-dan Mao ^d

Interplanetary Laser Tri-lateration Network

- Laser transponders based on LISA technology
- Asynchronous ranging



(Mazarico 2023)



(Smith et al. 2018)

Interplanetary Laser Tri-lateration Network

(Smith et al. 2018) : GM-dot of 10^{-14} over 5 years

Scientific Rational

Loss of solar mass by internal nuclear reactions

Change in the gravitational constant, $G\text{-dot}/G$

Test of equivalence principle

Expansion of the solar system

Lense-Thirring precession of reference frame

Relativistic parameters, β & γ

Gravitational flattening of the sun, J_2

Precession, nutation & rotation of host planets

Obliquity, tides, moment of inertia of host planets

Low-degree gravity, seasonal change on host planets

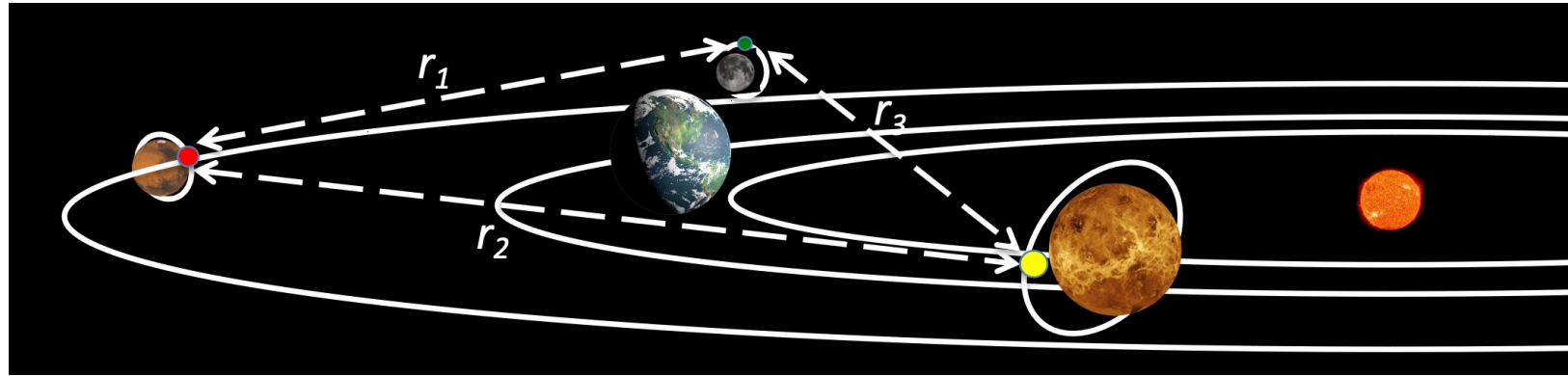
Inferences on interior structure

Orbits of host planets

Interplanetary Laser Tri-lateration Network

(Smith et al. 2018) : GM-dot of 10^{-14} over 5 years

ILTN



- 3 spacecraft, orbiting 3 planets, ~ 200 millions km apart connected by ranging measurements.
- Accuracy ~ 1 cm for one single measurement
- at a cadence of 1 measurement per second
- continued for 1 day (86400 s) \rightarrow diurnal normal point

Sensitivity analysis

(Bills 2023)

If we use parameter values

$$\varepsilon = 1 \text{ cm}$$

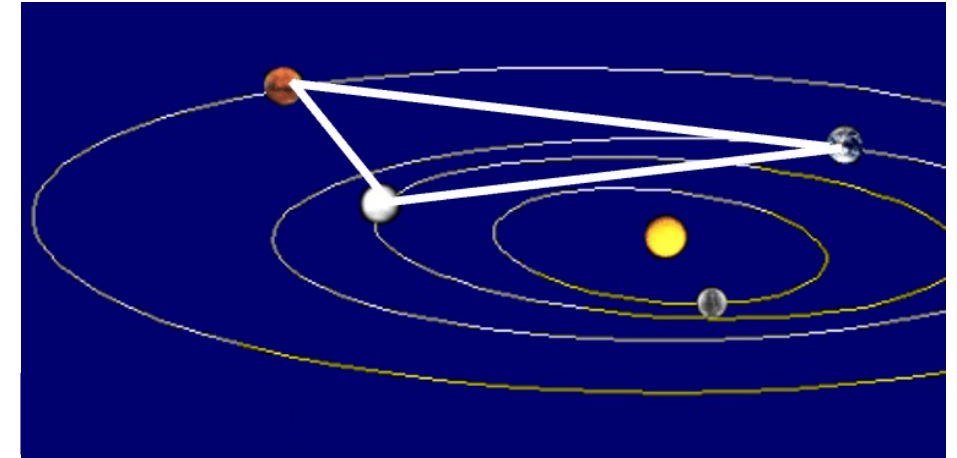
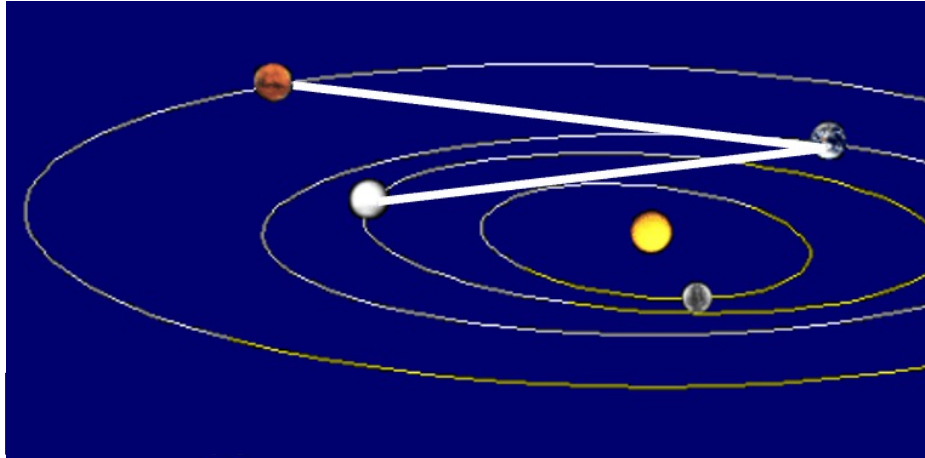
$$N = 86400 \text{ (seconds/day)}$$

the resulting diurnal RMS error values are

$$\sigma[a] \sim \varepsilon \sqrt{\frac{9}{N}} = 1.04 \cdot 10^{-6} \text{ m}$$

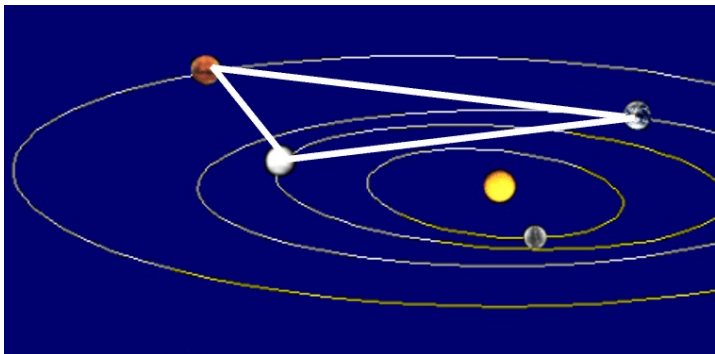
$$\sigma[b] \sim \varepsilon \sqrt{\frac{192}{N^3}} = 2.57 \cdot 10^{-10} \text{ m/s}$$

$$\sigma[c] \sim \varepsilon \sqrt{\frac{180}{N^5}} = 2.79 \cdot 10^{-15} \text{ m/s}^2$$



- With and without Venus-Mars link
- Durations: 1 year, 2.5 years and 5 years
- 1 normal point per day with 0.1 mm accuracy

Impact of the mission duration for 0.1 mm with Venus-Mars link

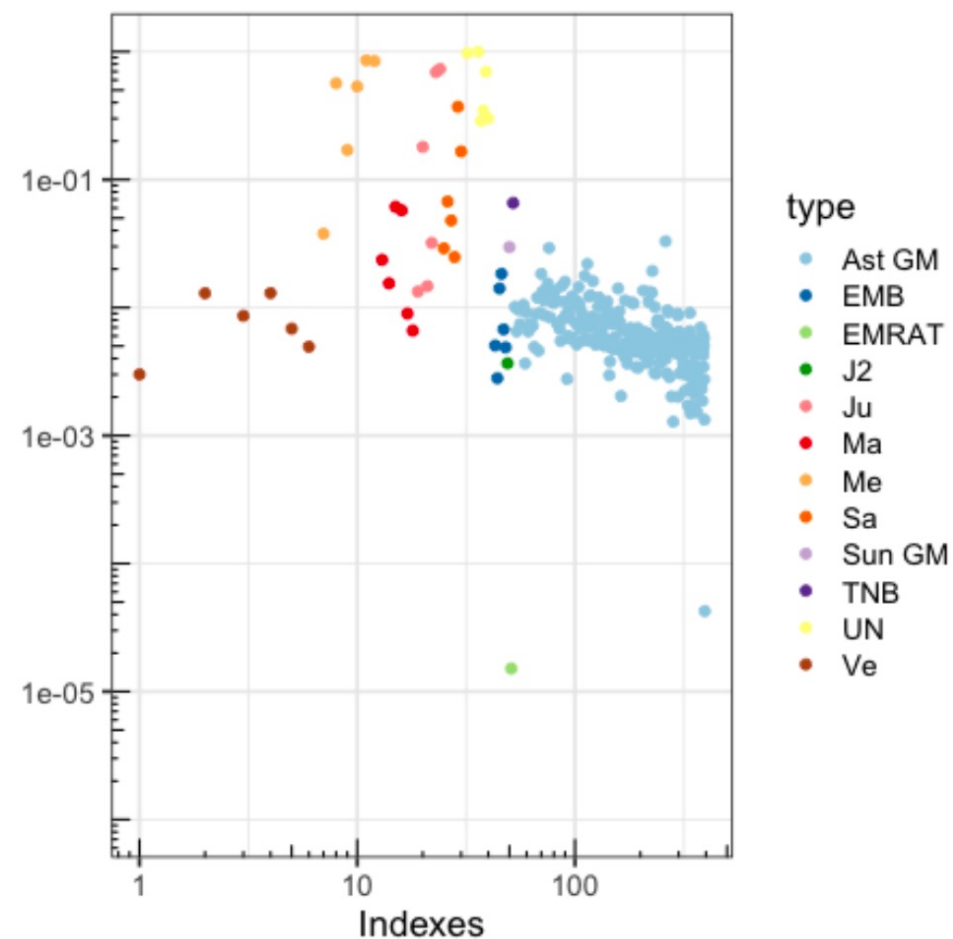
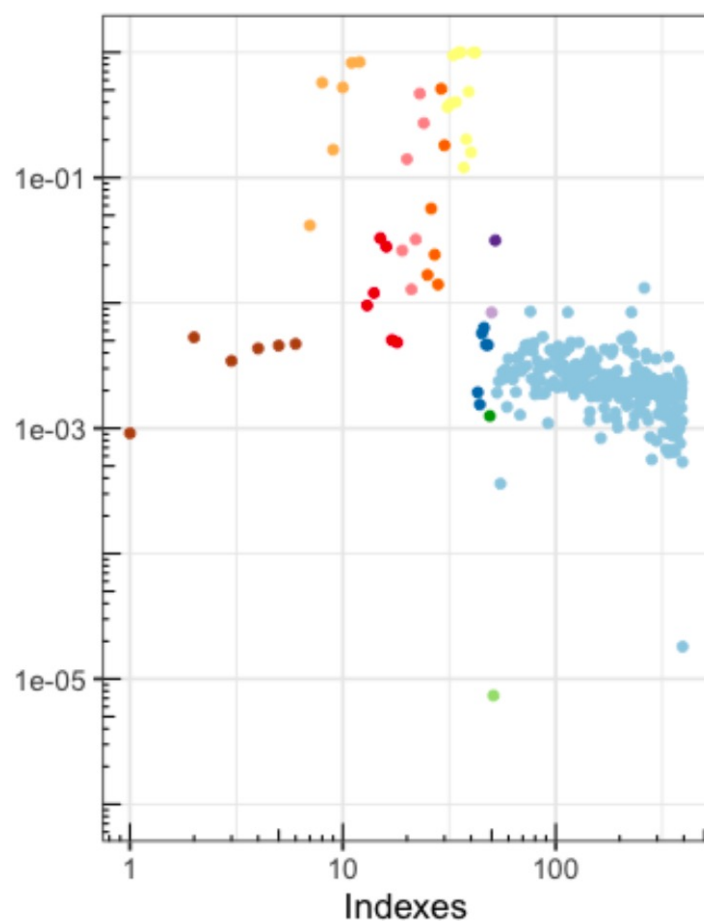
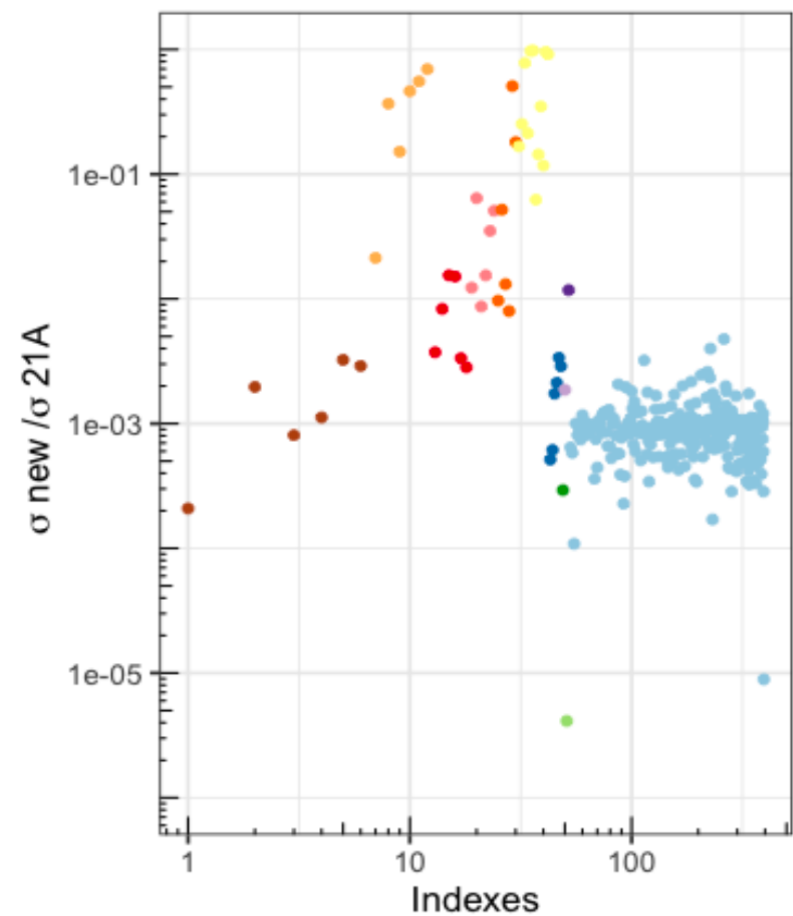


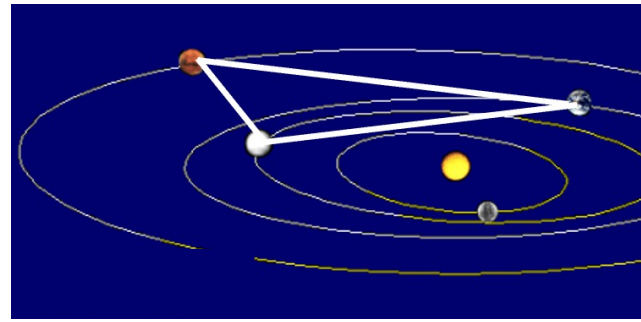
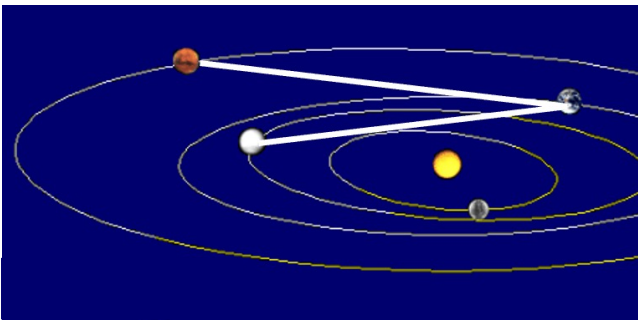
Conclusion A: 1 order improvement from 1 to 5 yrs mission

Duration: 5 years

Duration: 2.5 years

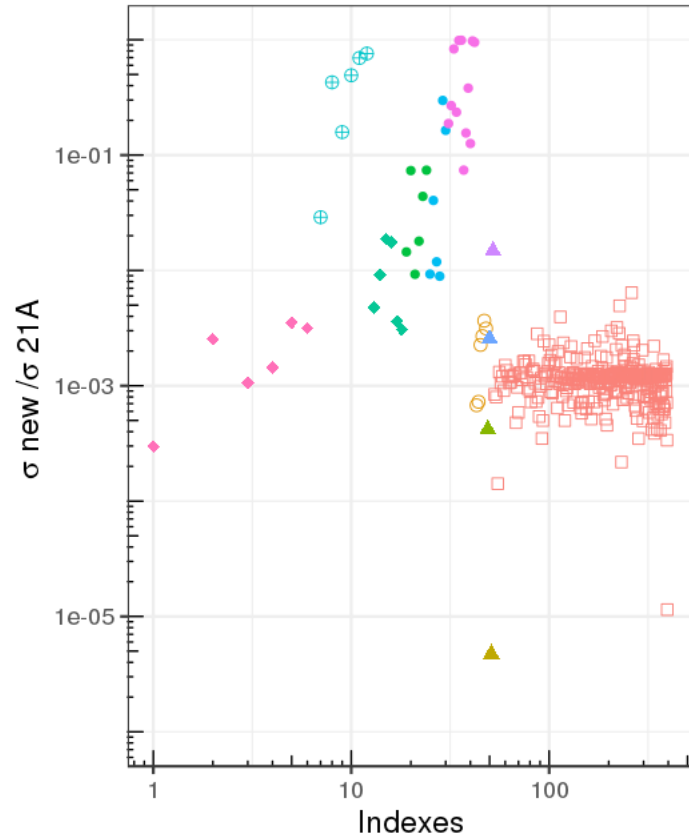
Duration: 1 years



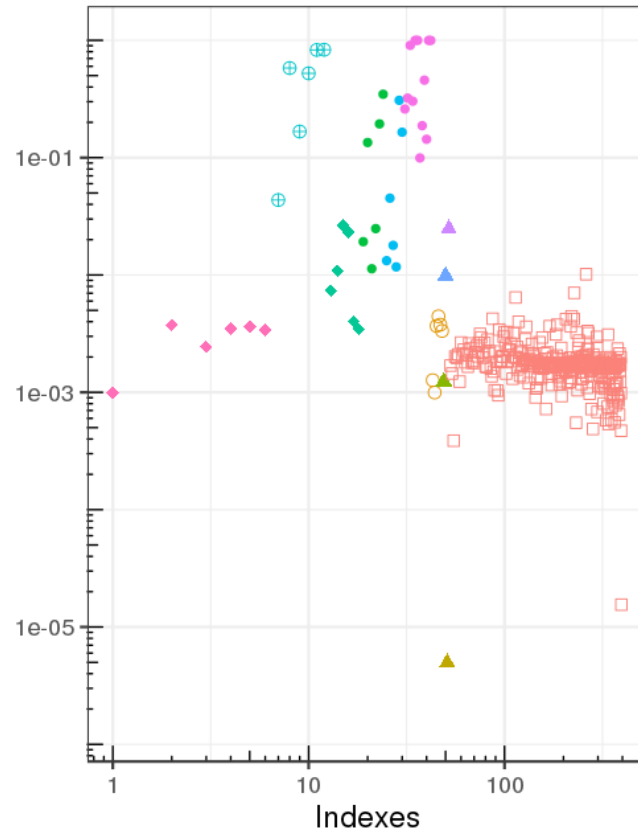


Conclusion B: Factor 2 improvement with Venus-Mars link

VE + ME + VM @ 0.1 mm for 5 years



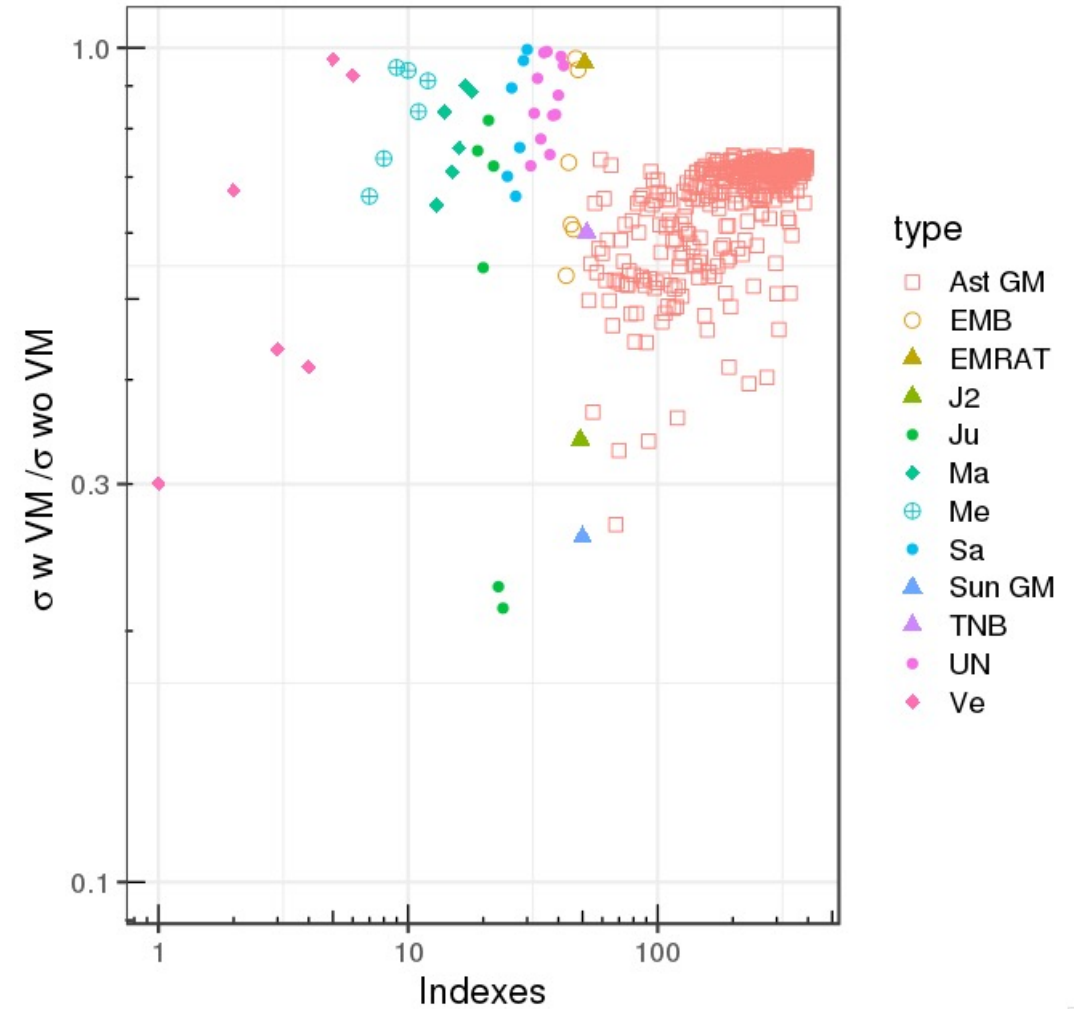
VE + ME @ 0.1 mm for 5 years



Impact of the Venus-Mars link
for 0.1 mm

Duration: 5 years

Impact of Venus-Mars link

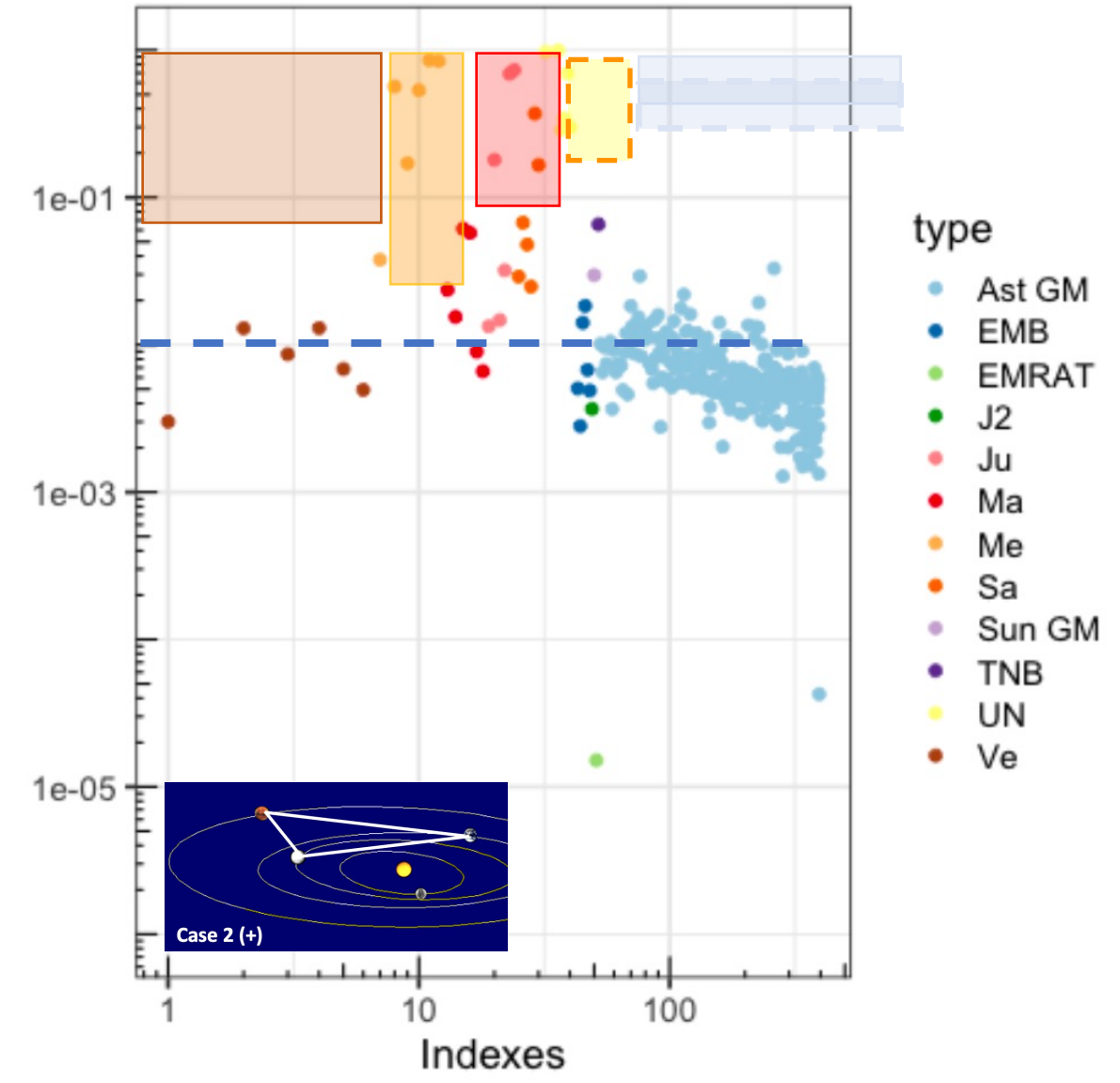
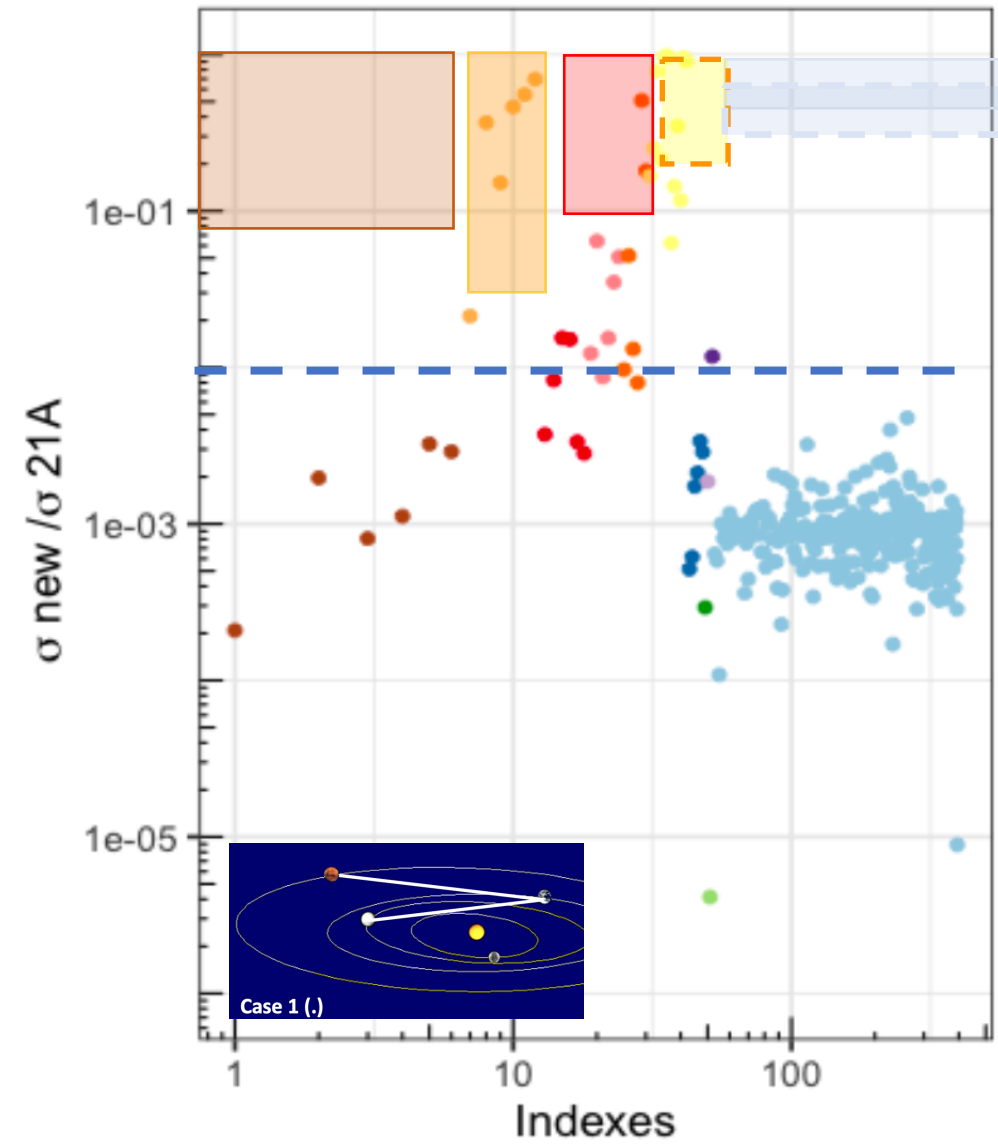


Comparison with BC/JUICE

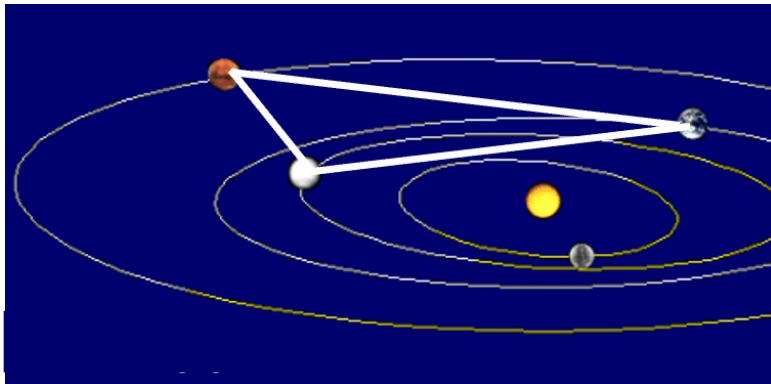
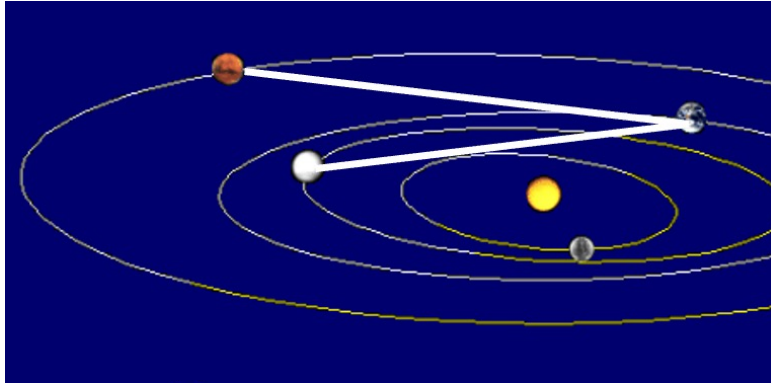
- Duration: 5 years
- Accuracy : 0.1 mm
- Without Venus-Mars link

Conclusion C: Interesting in particular for MB asteroids

- Duration: 1 years
- Accuracy : 0.1 mm
- With Venus-Mars link



Ratio of covariances for $\dot{\mu}/\mu$ estimated together with other planetary ephemeris parameters



	VE+ME+VM 0.1 mm	VE+ME 0.1 mm	VE+ME+V M 1 cm
5 yrs	0.001	0.0018	0.55
2.5 yrs	0.003	0.0045	0.66
1 yrs	0.009	0.012	0.75

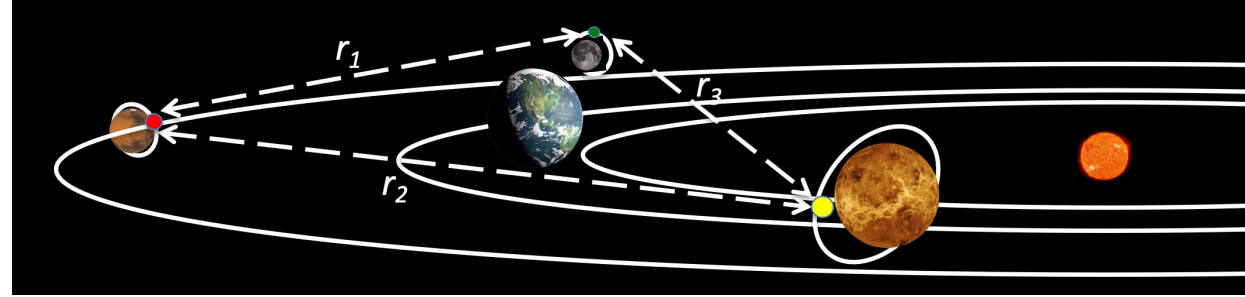
Present measurement (INPOP21a) = $6 \times 10^{-13} \text{ yr}^{-1}$

Ratio with Bepi-Colombo (2yrs @ 1 cm) = 0.17

Conclusion D: Significant improvement for $\dot{\mu}/\mu$

No BC nor EC/JUICE data included

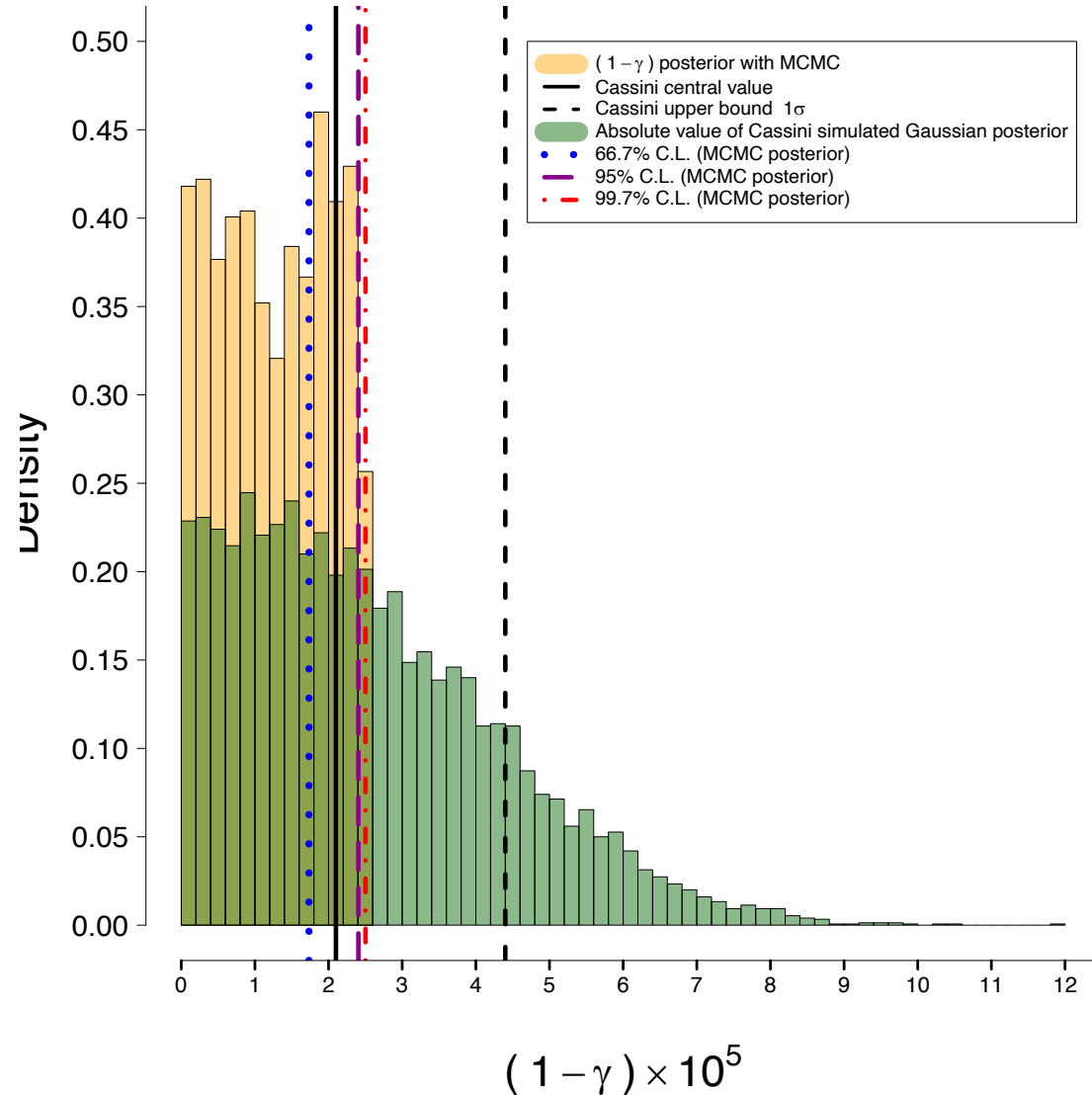
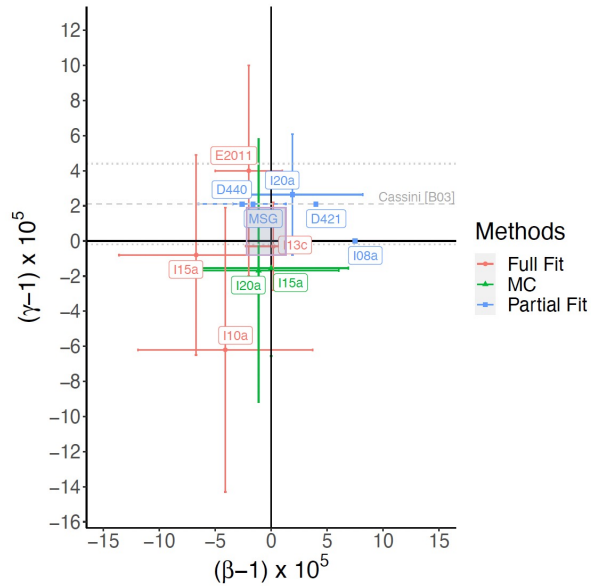
Interplanetary Laser Tri-lateration Network : conclusions



- Another meeting is planned for first semester 2024
- Technological challenges seem significant (LISA heritage)

fin

Test A: MCMC on γ in PPN (without SEP, $\delta_A = 0$)



$$|1 - \gamma| < 2.5 \times 10^{-5} \text{ (99.7\%)}$$

(Bertotti et al. 2003)

$$(1 - \gamma) = (-2.1 \pm 2.3) \times 10^{-5}$$

$$(\beta - 1) = (-0.45 \pm 1.75) \times 10^{-5}$$

$$(\gamma - 1) = (0.55 \pm 1.35) \times 10^{-5}$$